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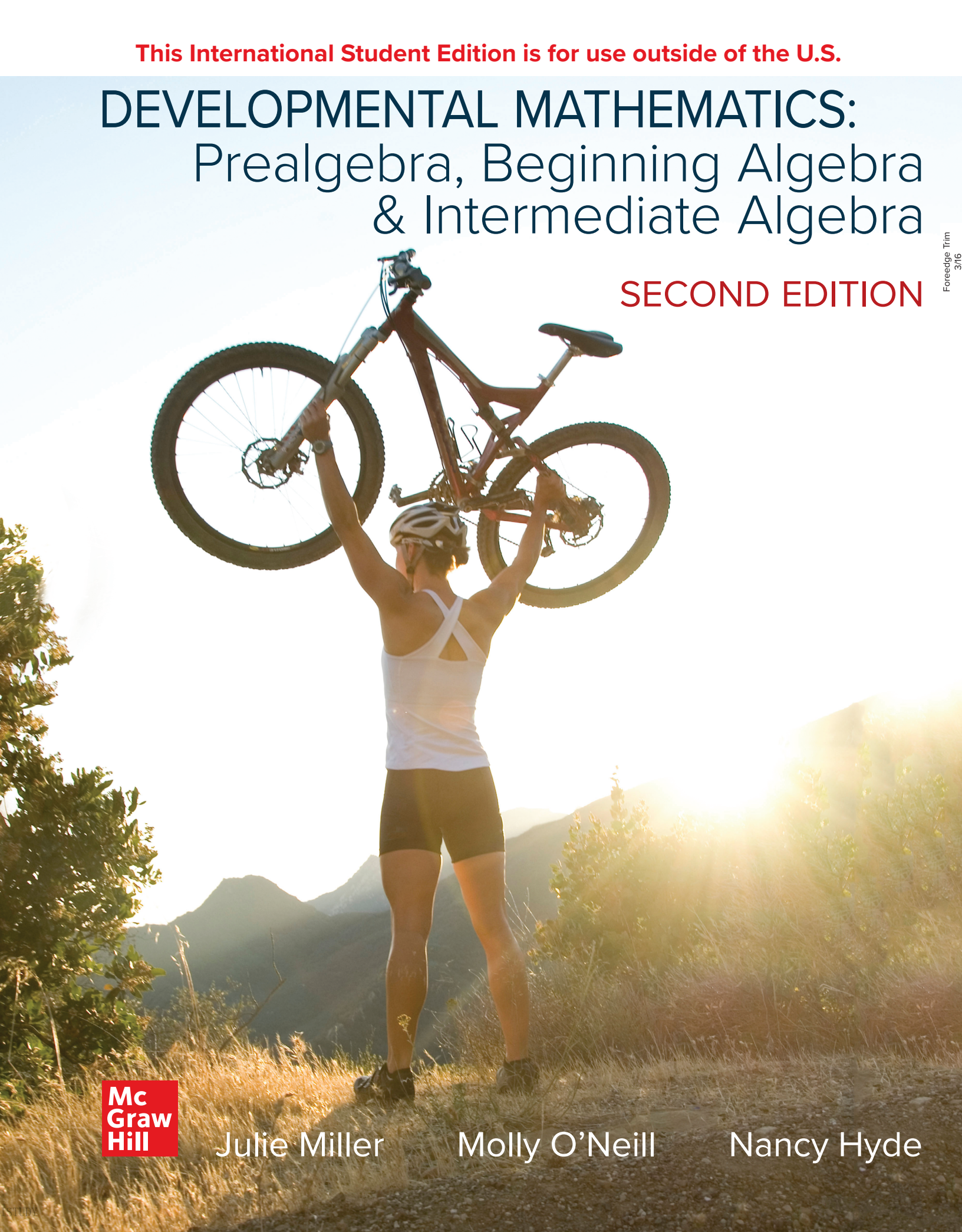
DEVELOPMENTAL MATHEMATICS: Prealgebra, Beginning Algebra & Intermediate Algebra

SECOND EDITION



Julie Miller Molly O'Neill Nancy Hyde

DEVELOPMENTAL MATHEMATICS: Prealgebra, Beginning Algebra, & Intermediate Algebra

SECOND EDITION

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Mc Graw Hill

DEVELOPMENTAL MATHEMATICS

This book is printed on acid-free paper.

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Letter from the Authors

Dear Colleagues,

Across the country, Developmental Math courses are in a state of flux, and we as instructors are at the center of it all. As many of our institutions are grappling with the challenges of placement, retention, and graduation rates, we are on the front lines with our students—supporting all of them in their educational journey.

Flexibility—No Matter Your Course Format!

The three of us each teach differently, as do many of our current users. The Miller/O'Neill/Hyde series is designed for successful use in a variety of course formats, both traditional and modern—classroom lecture settings, flipped classrooms, hybrid classes, and online-only classes.

Ease of Instructor Preparation

We've all had to fill in for a colleague, pick up a last-minute section, or find ourselves running across campus to yet a different course. The Miller/O'Neill/Hyde series is carefully designed to support instructors teaching in a variety of different settings and circumstances. Experienced, senior faculty members can draw from a massive library of static and algorithmic content found in ALEKS to meticulously build assignments and assessments sharply tailored to individual student needs. Newer instructors and part-time adjunct instructors, on the other hand, will find support through a wide range of digital resources and prebuilt assignments ready to go on Day One. With these tools, instructors with limited time to prepare for class can still facilitate successful student outcomes.

Many instructors want to incorporate discovery-based learning and groupwork into their courses but don't have time to write or find quality materials. Each section of the text has numerous discovery-based activities that we have tested in our own classrooms. These are found in the text and Student Resource Manual along with other targeted worksheets for additional practice and materials for a student portfolio.

Student Success—Now and in the Future

Too often our math placement tests fail our students, which can lead to frustration, anxiety, and often withdrawal from their education journey. We encourage you to learn more about ALEKS Placement, Preparation, and Learning (ALEKS PPL), which uses adaptive learning technology to place students appropriately. No matter the skills they come in with, the Miller/O'Neill/Hyde series provides resources and support that uniquely position them for success in that course and for their next course. Whether they need a brush-up on their basic skills, ADA supportive materials, or advanced topics to help them cross the bridge to the next level, we've created a support system for them.

We hope you are as excited as we are about the series and the supporting resources and services that accompany it. Please reach out to any of us with any questions or comments you have about our texts.

Julie Miller Molly O'Neill Nancy Hyde

About the Authors

Photo courtesy of Molly O'Neill

Julie Miller is from Daytona State College, where she taught developmental and upper-level mathematics courses for 20 years. Prior to her work at Daytona State College, she worked as a software engineer for General Electric in the area of flight and radar simulation. Julie earned a Bachelor of Science in Applied Mathematics from Union College in Schenectady, New York, and a Master of Science in Mathematics from the University of Florida. In addition to this textbook, she has authored textbooks for college algebra, trigonometry, and precalculus, as well as several short works of fiction and nonfiction for young readers.

"My father is a medical researcher, and I got hooked on math and science when I was young and would visit his laboratory. I can remember using graph paper to plot data points for his experiments and doing simple calculations. He would then tell me what the peaks and features in the graph meant in the context of his experiment. I think that applications and hands-on experience made math come alive for me, and I'd like to see math come alive for my students."

—Julie Miller

Molly O'Neill is also from Daytona State College, where she taught for 22 years in the School of Mathematics. She has taught a variety of courses from developmental mathematics to calculus. Before she came to Florida, Molly taught as an adjunct instructor at the University of Michigan–Dearborn, Eastern Michigan University, Wayne State University, and Oakland Community College. Molly earned a Bachelor of Science in Mathematics and a Master of Arts and Teaching from Western Michigan University in Kalamazoo, Michigan. Besides this textbook, she has authored several course supplements for college algebra, trigonometry, and precalculus and has reviewed texts for developmental mathematics.

"I differ from many of my colleagues in that math was not always easy for me. But in seventh grade I had a teacher who taught me that if I follow the rules of mathematics, even I could solve math problems. Once I understood this, I enjoyed math to the point of choosing it for my career. I now have the greatest job because I get to do math every day and I have the opportunity to influence my students just as I was influenced. Authoring these texts has given me another avenue to reach even more students."

—Molly O'Neill

Nancy Hyde served as a full-time faculty member of the Mathematics Department at Broward College for 24 years. During this time she taught the full spectrum of courses from developmental math through differential equations. She received a Bachelor of Science in Math Education from Florida State University and a Master's degree in Math Education from Florida Atlantic University. She has conducted workshops and seminars for both students and teachers on the use of technology in the classroom. In addition to this textbook, she has authored a graphing calculator supplement for *College Algebra*.

"I grew up in Brevard County, Florida, where my father worked at Cape Canaveral. I was always excited by mathematics and physics in relation to the space program. As I studied higher levels of mathematics I became more intrigued by its abstract nature and infinite possibilities. It is enjoyable and rewarding to convey this perspective to students while helping them to understand mathematics."

—Nancy Hyde

Dedication

To Our Students

Julie Miller ⚜ Molly O'Neill ⚜ Nancy Hyde

The Miller/O'Neill/Hyde Developmental Math Series

Julie Miller, Molly O'Neill, and Nancy Hyde originally wrote their developmental math series because students were entering their College Algebra course underprepared. The students were not mathematically mature enough to understand the concepts of math, nor were they fully engaged with the material. The authors began their developmental mathematics offerings with Intermediate Algebra to help bridge that gap. This in turn evolved into several series of textbooks from Prealgebra through Precalculus to help students at all levels before Calculus.

What sets all of the Miller/O'Neill/Hyde series apart is that they address course content through an author-created digital package that maintains a consistent voice and notation throughout the program. This consistency—in videos, PowerPoints, Lecture Notes, and Integrated Video and Study Guides—coupled with the power of ALEKS, ensures that students master the skills necessary to be successful in Developmental Math through Precalculus and prepares them for the Calculus sequence.

Developmental Math Series

The Developmental Math series is traditional in approach, delivering a purposeful balance of skills and conceptual development. It places a strong emphasis on conceptual learning to prepare students for success in subsequent courses.

Basic College Mathematics, Third Edition
Prealgebra, Third Edition
Prealgebra & Introductory Algebra, Second Edition
Beginning Algebra, Sixth Edition
Beginning & Intermediate Algebra, Sixth Edition
Intermediate Algebra, Sixth Edition
Developmental Mathematics: Prealgebra, Beginning Algebra, & Intermediate Algebra, Second Edition

The Miller/Gerken College Algebra/Precalculus Series

The Precalculus series serves as the bridge from Developmental Math coursework to future courses by emphasizing the skills and concepts needed for Calculus.

College Algebra with Corequisite Support, First Edition
College Algebra, Second Edition
College Algebra and Trigonometry, First Edition
Precalculus, First Edition

Acknowledgments

The author team most humbly would like to thank all the people who have contributed to this project and the Miller/O'Neill/Hyde Developmental Math series as a whole.

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We also greatly appreciate the many people behind the scenes at McGraw Hill without whom we would still be on page 1. To Megan Platt, our product developer: thank you for being our help desk and handling all things math, English, and editorial. To Brittney Merriman and Jennifer Morales, our portfolio managers and team leaders: thank you so much for leading us down this path. Your insight, creativity, and commitment to our project has made our job easier.

To the marketing team, Michele McTighe, Noah Evans, and Mary Ellen Rahn: thank you for your creative ideas in making our books come to life in the market. Thank you as well to Debbie McFarland, Justin Washington, and Sherry Bartel for continuing to drive our long-term content vision through their market development efforts. And many thanks to the team at ALEKS for creating its spectacular adaptive technology and for overseeing the quality control.

To the production team: Jane Mohr, David Hash, Lorraine Buczek, and Sandy Ludovissy—thank you for making the manuscript beautiful and for keeping the unruly authors on track. To our copyeditor Kevin Campbell and proofreader John Murdzek, who have kept a watchful eye over our manuscripts—the two of you are brilliant. To our compositor Manvir Singh and his team at Aptara, you've been a dream to work with. And finally, to Kathleen McMahon and Caroline Celano, thank you for supporting our projects for many years and for the confidence you've always shown in us.

Most importantly, we give special thanks to the students and instructors who use our series in their classes.

Julie Miller
Molly O'Neill
Nancy Hyde

Contents

To the Student

Take a deep breath and know that you aren't alone. Your instructor, fellow students, and we, your authors, are here to help you learn and master the material for this course and prepare you for future courses. You may feel like math just isn't your thing, or maybe it's been a long time since you've had a math class—that's okay!

We wrote the text and all the supporting materials with you in mind. Most of our students aren't really sure how to be successful in math, but we can help with that.

As you begin your class, we'd like to offer some specific suggestions:

1. **Attend class.** Arrive on time and be prepared. If your instructor has asked you to read prior to attending class—do it. How often have you sat in class and thought you understood the material, only to get home and realize you don't know how to get started? By reading and trying a couple of Skill Practice exercises, which follow each example, you will be able to ask questions and gain clarification from your instructor when needed.
2. **Be an *active* learner.** Whether you are at lecture, watching an author lecture or exercise video, or are reading the text, pick up a pencil and work out the examples given. Math is learned only by doing; we like to say, "Math is not a spectator sport." If you like a bit more guidance, we encourage you to use the Integrated Video and Study Guide. It was designed to provide structure and note-taking for lectures and while watching the accompanying videos.
3. **Schedule time to do some math every day.** Exercise, foreign language study, and math are three things that you must do every day to get the results you want. If you are used to cramming and doing all of your work in a few hours on a weekend, you should know that even mathematicians start making silly errors after an hour or so! Check your answers. Skill Practice exercises all have the answers at the bottom of that page. Odd-numbered exercises throughout the text have answers in the back of the text. If you didn't get it right, don't throw in the towel. Try again, revisit an example, or bring your questions to class for extra help.
4. **Prepare for quizzes and exams.** Each chapter has a set of Chapter Review Exercises at the end to help you integrate all of the important concepts. In addition, there is a detailed Chapter Summary and a Chapter Test located in the online resources. If you use ALEKS, use all of the tools available within the program to test your understanding.
5. **Use your resources.** This text comes with numerous supporting resources designed to help you succeed in this class and in your future classes. Additionally, your instructor can direct you to resources within your institution or community. Form a student study group. Teaching others is a great way to strengthen your own understanding, and they might be able to return the favor if you get stuck.

We wish you all the best in this class and in your educational journey!

Julie Miller Molly O'Neill Nancy Hyde

Student Guide to the Text

Clear, Precise Writing

Learning from our own students, we have written this text in simple and accessible language. Our goal is to keep you engaged and supported throughout your coursework.

Call-Outs

Just as your instructor will share tips and math advice in class, we provide call-outs throughout the text to offer tips and warn against common mistakes.

- Tip boxes offer additional insight into a concept or procedure.
- Avoiding Mistakes help fend off common student errors.
- For Review boxes positioned strategically throughout the text remind students of key skills relating to the current topic.

Examples

- Each example is step-by-step, with thorough annotation to the right explaining each step.
- Following each example is a similar **Skill Practice** exercise to give you a chance to test your understanding. You will find the answer at the bottom of the page—providing a quick check.

Exercise Sets

Each type of exercise is built so you can successfully learn the materials and show your mastery on exams.

- **Activities for discovery-based learning** appear before the exercise sets to walk students through the concepts presented in each section of the text.
- **Study Skills Exercises** integrate your studies of math concepts with strategies for helping you grow as a student overall.
- **Vocabulary and Key Concept Exercises** check your understanding of the language and ideas presented within the section.
- **Prerequisite Review** exercises keep fresh your knowledge of math content already learned by providing practice with concepts explored in previous sections.
- **Concept Exercises** assess your comprehension of the specific math concepts presented within the section.
- **Mixed Exercises** evaluate your ability to successfully complete exercises that combine multiple concepts presented within the section.
- **Expanding Your Skills** challenge you with advanced skills practice exercises around the concepts presented within the section.
- **Problem Recognition Exercises** appear in strategic locations in each chapter of the text. These will require you to distinguish between similar problem types and to determine what type of problem-solving technique to apply.
- **Technology Exercises** appear where appropriate.

End-of-Chapter Materials

The features at the end of each chapter and online are perfect for reviewing before test time.

- **Chapter Review Exercises** provide additional opportunities to practice material from the entire chapter.
- **Section-by-section summaries** provide references to key concepts, examples, and vocabulary.
- **Chapter tests** are an excellent way to test your complete understanding of the chapter concepts.

How Will Miller/O'Neill/Hyde Help Your Students *Get Better Results?*

Clarity, Quality, and Accuracy

Julie Miller, Molly O'Neill, and Nancy Hyde know what students need to be successful in mathematics. Better results come from clarity in their exposition, quality of step-by-step worked examples, and accuracy of their exercise sets; but it takes more than just great authors to build a textbook series to help students achieve success in mathematics. Our authors worked with a strong team of mathematics instructors from around the country to ensure that the clarity, quality, and accuracy you expect from the Miller/O'Neill/Hyde series was included in this edition.

Exercise Sets

Comprehensive sets of exercises are available for every student level. Julie Miller, Molly O'Neill, and Nancy Hyde worked with a board of advisors from across the country to offer the appropriate depth and breadth of exercises for your students. **Problem Recognition Exercises** were created to improve student performance while testing.

Practice exercise sets help students progress from skill development to conceptual understanding. Student tested and instructor approved, the Miller/O'Neill/Hyde exercise sets will help your students *get better results*.

- **Activities for Discovery-Based Learning**
- **Prerequisite Review Exercises**
- **Problem Recognition Exercises**
- **Skill Practice Exercises**
- **Study Skills Exercises**
- **Mixed Exercises**
- **Expanding Your Skills Exercises**
- **Vocabulary and Key Concepts Exercises**
- **Technology Exercises**

Step-By-Step Pedagogy

This text provides enhanced step-by-step learning tools to help students *get better results*.

- **For Review** tips placed in the margin guide students back to related prerequisite skills needed for full understanding of course-level topics.
- **Worked Examples** provide an "easy-to-understand" approach, clearly guiding each student through a step-by-step approach to master each practice exercise for better comprehension.
- **TIPs** offer students extra cautious direction to help improve understanding through hints and further insight.
- **Avoiding Mistakes** boxes alert students to common errors and provide practical ways to avoid them. Both of these learning aids will help students get better results by showing how to work through a problem using a clearly defined step-by-step methodology that has been class tested and student approved.

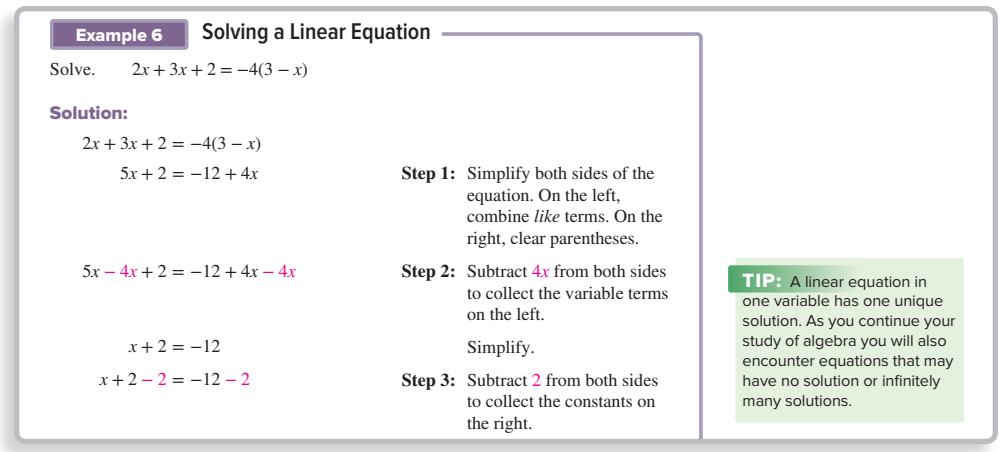
Get Better Results

Formula for Student Success

Step-by-Step Worked Examples

- Do you get the feeling that there is a disconnect between your students' class work and homework?
- Do your students have trouble finding worked examples that match the practice exercises?
- Do you prefer that your students see examples in the textbook that match the ones you use in class?

Miller/O'Neill/Hyde's *Worked Examples* offer a clear, concise methodology that replicates the mathematical processes used in the authors' classroom lectures.



Example 6 Solving a Linear Equation

Solve. $2x + 3x + 2 = -4(3 - x)$

Solution:

$2x + 3x + 2 = -4(3 - x)$

$5x + 2 = -12 + 4x$ — **Step 1:** Simplify both sides of the equation. On the left, combine *like* terms. On the right, clear parentheses.

$5x - 4x + 2 = -12 + 4x - 4x$ — **Step 2:** Subtract $4x$ from both sides to collect the variable terms on the left.

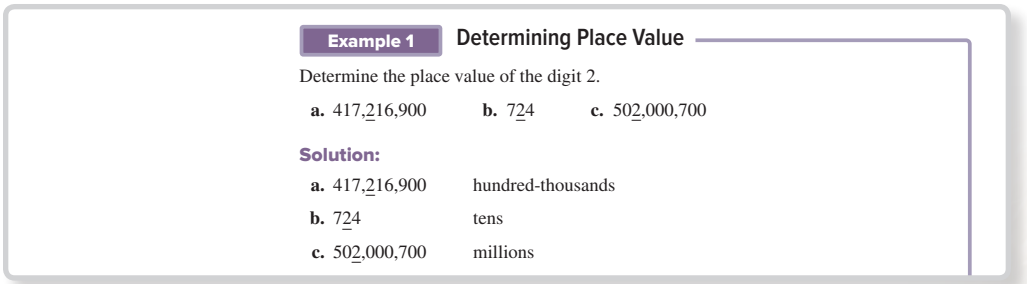
$x + 2 = -12$ — Simplify.

$x + 2 - 2 = -12 - 2$ — **Step 3:** Subtract 2 from both sides to collect the constants on the right.

TIP: A linear equation in one variable has one unique solution. As you continue your study of algebra you will also encounter equations that may have no solution or infinitely many solutions.

Classroom Examples

To ensure that the classroom experience also matches the examples in the text and the practice exercises, we have included references to even-numbered exercises to be used as Classroom Examples. These exercises are highlighted in the Practice Exercises at the end of each section.



Example 1 Determining Place Value

Determine the place value of the digit 2.

a. 417,216,900 **b.** 724 **c.** 502,000,700

Solution:

a. 417,216,900 hundred-thousands

b. 724 tens

c. 502,000,700 millions

Quality Learning Tools

For Review Boxes

Throughout the text, just-in-time tips and reminders of prerequisite skills appear in the margin alongside the concepts for which they are needed. References to prior sections are given for cases where more comprehensive review is available earlier in the text.

FOR REVIEW

Recall that addition may be performed in any order.

200 ft
200 ft
300 ft
275 ft
+ 475 ft
1450 ft

TIP and Avoiding Mistakes Boxes

TIP and **Avoiding Mistakes** boxes have been created based on the authors' classroom experiences—they have also been integrated into the **Worked Examples.** These pedagogical tools will help students get better results by learning how to work through a problem using a clearly defined step-by-step methodology.

Example 6 Simplifying Expressions

Simplify.

a. $-(-9)$ **b.** $-|-12|$ **c.** $-|7|$

Solution:

a. $-(-9) = 9$ This represents the opposite of -9, which is 9.

b. $-|-12| = -12$ This represents the opposite of $|-12|$. Since $|-12|$ is equal to 12, the opposite is -12.

c. $-|7| = -7$ This represents the opposite of $|7|$. Since $|7|$ is equal to 7, the opposite is -7.

Avoiding Mistakes

In Example 6(b) two operations are performed. First take the absolute value of -12. Then determine the opposite of the result.

Skill Practice Simplify.

15. $-(-34)$ **16.** $-|-20|$ **17.** $-|4|$

Answers

13. 108 **14.** -54
15. 34 **16.** -20 **17.** -4

Avoiding Mistakes Boxes:

Avoiding Mistakes boxes are integrated throughout the textbook to alert students to common errors and how to avoid them.

TIP: To simplify square roots, it is advisable to become familiar with these squares and square roots.

$0^2 = 0 \longrightarrow \sqrt{0} = 0$ $\quad 7^2 = 49 \longrightarrow \sqrt{49} = 7$

$1^2 = 1 \longrightarrow \sqrt{1} = 1$ $\quad 8^2 = 64 \longrightarrow \sqrt{64} = 8$

$2^2 = 4 \longrightarrow \sqrt{4} = 2$ $\quad 9^2 = 81 \longrightarrow \sqrt{81} = 9$

$3^2 = 9 \longrightarrow \sqrt{9} = 3$ $\quad 10^2 = 100 \longrightarrow \sqrt{100} = 10$

$4^2 = 16 \longrightarrow \sqrt{16} = 4$ $\quad 11^2 = 121 \longrightarrow \sqrt{121} = 11$

$5^2 = 25 \longrightarrow \sqrt{25} = 5$ $\quad 12^2 = 144 \longrightarrow \sqrt{144} = 12$

$6^2 = 36 \longrightarrow \sqrt{36} = 6$ $\quad 13^2 = 169 \longrightarrow \sqrt{169} = 13$

TIP Boxes

Teaching tips are usually revealed only in the classroom. Not anymore! TIP boxes offer students helpful hints and extra direction to help improve understanding and provide further insight.

Get Better Results

Better Exercise Sets and Better Practice Yield Better Results

- Do your students have trouble with problem solving?
- Do you want to help students overcome math anxiety?
- Do you want to help your students improve performance on math assessments?

Problem Recognition Exercises

Problem Recognition Exercises present a collection of problems that look similar to a student upon first glance, but are actually quite different in the manner of their individual solutions. Students sharpen critical thinking skills and better develop their "solution recall" to help them distinguish the method needed to solve an exercise—an essential skill in mathematics.

Problem Recognition Exercises were tested in the authors' developmental mathematics classes and were created to improve student performance on tests.

Problem Recognition Exercises

Operations on Whole Numbers

For Exercises 1–14, perform the indicated operations.

1. a. $\begin{array}{r} 96 \\ +\ 24 \\ \hline \end{array}$	**b.** $\begin{array}{r} 96 \\ -\ 24 \\ \hline \end{array}$	**c.** $\begin{array}{r} 96 \\ \times\ 24 \\ \hline \end{array}$	**d.** $24\overline{)96}$
2. a. $\begin{array}{r} 550 \\ +\ 25 \\ \hline \end{array}$	**b.** $\begin{array}{r} 550 \\ -\ 25 \\ \hline \end{array}$	**c.** $\begin{array}{r} 550 \\ \times\ 25 \\ \hline \end{array}$	**d.** $25\overline{)550}$
3. a. $\begin{array}{r} 612 \\ +\ 334 \\ \hline \end{array}$	**b.** $\begin{array}{r} 946 \\ -\ 334 \\ \hline \end{array}$	**4. a.** $\begin{array}{r} 612 \\ -\ 334 \\ \hline \end{array}$	**b.** $\begin{array}{r} 278 \\ +\ 334 \\ \hline \end{array}$
5. a. $\begin{array}{r} 5500 \\ -\ 4299 \\ \hline \end{array}$	**b.** $\begin{array}{r} 1201 \\ +\ 4299 \\ \hline \end{array}$	**6. a.** $\begin{array}{r} 22{,}718 \\ +\ 12{,}137 \\ \hline \end{array}$	**b.** $\begin{array}{r} 34{,}855 \\ -\ 12{,}137 \\ \hline \end{array}$
7. a. $50 \cdot 400$	**b.** $20{,}000 \div 50$	**8. a.** $548 \cdot 63$	**b.** $34{,}524 \div 63$
9. a. $5060 \div 22$	**b.** $230 \cdot 22$	**10. a.** $1875 \div 125$	**b.** $125 \cdot 15$
11. a. $4\overline{)1312}$	**b.** $328\overline{)1312}$	**12. a.** $547\overline{)4376}$	**b.** $8\overline{)4376}$
13. a. $418 \cdot 10$	**b.** $418 \cdot 100$	**c.** $418 \cdot 1000$	**d.** $418 \cdot 10{,}000$
14. a. $350{,}000 \div 10$	**b.** $350{,}000 \div 100$	**c.** $350{,}000 \div 1000$	**d.** $350{,}000 \div 10{,}000$

Get Better Results

Student-Centered Applications

The Miller/O'Neill/Hyde Board of Advisors partnered with our authors to bring the *best applications* from every region in the country! These applications include real data and topics that are more relevant and interesting to today's student.

24. Liu earned $312 on an investment of $800. How much would $1100 have earned in the same investment?

25. A skyscraper in Chicago is 1454 ft high. If a model is made in which 1 in. represents 50 ft, how high would the building be in the model?

Activities

Each section of the text ends with an activity that steps the student through the major concepts of the section. The purpose of the activities is to promote active, discovery-based learning for the student. The implementation of the activities is flexible for a variety of delivery methods. For face-to-face classes, the activities can be used to break up lecture by covering the exercises intermittently during the class. For the flipped classroom and hybrid classes, students can watch the videos and try the activities. Then, in the classroom, the instructor can go over the activities or have the students compare their answers in groups. For online classes, the activities provide great discussion questions.

Section 1.1 Activity

A.1. In a recent presidential election, the State of Wisconsin had 1,902,505 people request an absentee ballot.
- **a.** Determine the place value of the underlined digit. 1,9̲02,505 _____
- **b.** Convert 1,902,505 to expanded form.
- **c.** Write 1,902,505 in words.

A.2. Of the 1,902,505 total absentee ballots requested in Wisconsin, one million, eight hundred ninety-six thousand, five hundred thirty-one ballots were sent to voters. Write this number in standard form.

For Exercises A.3–A.6:
- **a.** Write two true inequalities (one using > and one using <) for each pair of values given below.
- **b.** Translate one of the inequalities to words.

A.3. 210 and 201
- **a.** _____ or _____
- **b.** _____

A.4. 2233 and 2323
- **a.** _____ or _____
- **b.** _____

A.5. 79 and 76
- **a.** _____ or _____
- **b.** _____

A.6. 614 and 641
- **a.** _____ or _____
- **b.** _____

A.7. Consider the numbers 5, 9, 2, and 7.
- **a.** What is the greatest four-digit number that can be formed from the digits? Use each digit only once.
- **b.** What is the smallest four-digit number that can be formed from the digits? Use each digit only once.
- **c.** Write the number from part (b) in words.

Get Better Results

Additional Supplements

Lecture Videos Created by the Authors

Julie Miller began creating these lecture videos for her own students to use when they were absent from class. The student response was overwhelmingly positive, prompting the author team to create the lecture videos for their entire developmental math book series. In these videos, the authors walk students through the learning objectives using the same language and procedures outlined in the book. Students learn and review right alongside the author! Students can also access the written notes that accompany the videos.

Integrated Video and Study Workbooks

The Integrated Video and Study Workbooks were built to be used in conjunction with the Miller/O'Neill/Hyde Developmental Math series online lecture videos. These new video guides allow students to consolidate their notes as they work through the material in the book, and they provide students with an opportunity to focus their studies on particular topics that they are struggling with rather than entire chapters at a time. Each video guide contains written examples to reinforce the content students are watching in the corresponding lecture video, along with additional written exercises for extra practice. There is also space provided for students to take their own notes alongside the guided notes already provided. By the end of the academic term, the video guides will not only be a robust study resource for exams, but will serve as a portfolio showcasing the hard work of students throughout the term.

Dynamic Math Animations

The authors have constructed a series of animations to illustrate difficult concepts where static images and text fall short. The animations leverage the use of on-screen movement and morphing shapes to give students an interactive approach to conceptual learning. Some provide a virtual laboratory for which an application is simulated and where students can collect data points for analysis and modeling. Others provide interactive question-and-answer sessions to test conceptual learning.

Exercise Videos

The authors, along with a team of faculty who have used the Miller/O'Neill/Hyde textbooks for many years, have created exercise videos for designated exercises in the textbook. These videos cover a representative sample of the main objectives in each section of the text. Each presenter works through selected problems, following the solution methodology employed in the text.

The video series is available online as part of ALEKS 360. The videos are closed-captioned for the hearing impaired and meet the Americans with Disabilities Act Standards for Accessible Design.

Student Resource Manual

The *Student Resource Manual (SRM),* created by the authors, is a printable, electronic supplement available to students through ALEKS. Instructors can also choose to customize this manual and package it with their course materials. With increasing demands on faculty schedules, this resource offers a convenient means for both full-time and adjunct faculty to promote active learning and success strategies in the classroom.

This manual supports the series in a variety of different ways:

- Additional group activities developed by the authors to supplement what is already available in the text
- Discovery-based classroom activities written by the authors for each section
- Excel activities that not only provide students with numerical insights into algebraic concepts, but also teach simple computer skills to manipulate data in a spreadsheet

- Worksheets for extra practice written by the authors, including Problem Recognition Exercise Worksheets
- Lecture Notes designed to help students organize and take notes on key concepts
- Materials for a student portfolio

Annotated Instructor's Edition

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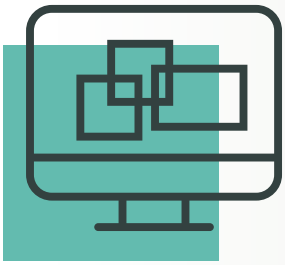

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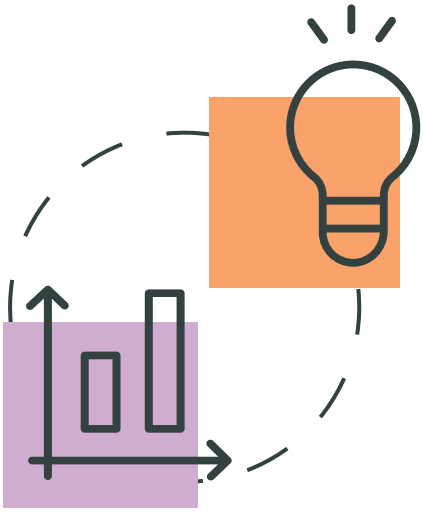

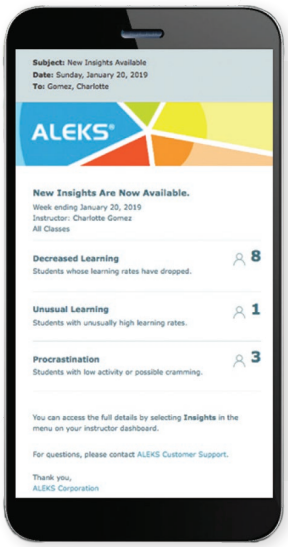

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Whole Numbers

1

CHAPTER OUTLINE

Numbers on Vacation

Since the beginning of human civilization, the need to communicate with one another in a precise, quantifiable language has become increasingly important. For example, to take a vacation to Disney World, a family would want to know the driving distance to the park, the time required to drive there, the cost for tickets, the number of nights for a hotel room, and the estimated amount spent on food and incidentals. Such numerical (quantifiable) information is essential for the family to determine if the vacation is affordable and to form a budget for the vacation.

Suppose the family lives 300 miles from Disney World, drives a car that gets 30 miles per gallon of gasoline, and travels 60 miles per hour. These numerical values are called whole numbers. Whole numbers include 0 and the counting numbers 1, 2, 3, and so on. Operations on whole numbers can help us solve a variety of applications. For example, dividing the whole number 300 miles by 30 miles per gallon tells us that the family will use 10 gallons of gasoline. Furthermore, dividing 300 miles by 60 miles per hour tells us that the family will arrive at Disney World in 5 hours. As you work through this chapter, reflect on how important numbers are to everyday living and how different our world would be without the precision of numerical values.

Ilene MacDonald/Alamy Stock Photo

Section 1.1 Introduction to Whole Numbers

Concepts

1. Place Value

Numbers provide the foundation that is used in mathematics. We begin this chapter by discussing how numbers are represented and named. All numbers in our numbering system are composed from the **digits** 0, 1, 2, 3, 4, 5, 6, 7, 8, and 9. In mathematics, the numbers 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, . . . are called the *whole numbers.* (The three dots are called *ellipses* and indicate that the list goes on indefinitely.)

For large numbers, commas are used to separate digits into groups of three called **periods**. For example, the number of live births in the United States in a recent year was 4,058,614. (*Source: The World Almanac*) Numbers written in this way are said to be in **standard form**. The position of each digit determines the place value of the digit. To interpret the number of births in the United States, refer to the place value chart (Figure 1-1).

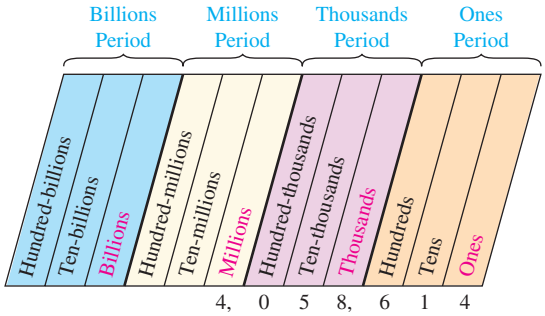

Figure 1-1

The digit 5 in 4,058,614 represents 5 ten-thousands because it is in the ten-thousands place. The digit 4 on the left represents 4 millions, whereas the digit 4 on the right represents 4 ones.

Example 1 Determining Place Value

Determine the place value of the digit 2.

a. 417,216,900 **b.** 724 **c.** 502,000,700

Solution:

a. 417,216,900 hundred-thousands

b. 724 tens

c. 502,000,700 millions

Skill Practice Determine the place value of the digit 4.

1. 547,098,632
2. 1,659,984,036
3. 6420

Answers

1. Ten-millions
2. Thousands
3. Hundreds

Example 2 **Determining Place Value**

The altitude of Mount Everest, the highest mountain on Earth, is 29,035 feet (ft). Give the place value for each digit.

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Solution:

29,035

- ones
- tens
- hundreds
- thousands
- ten-thousands

Skill Practice

4. Alaska is the largest state geographically. Its land area is 571,962 square miles (mi^2). Give the place value for each digit.

2. Standard Notation and Expanded Notation

A number can also be written in an expanded form by writing each digit with its place value unit. For example, 287 can be written as

$$\begin{aligned} 287 &= 2 \text{ hundreds} + 8 \text{ tens} + 7 \text{ ones} \\ &= 2 \times 100 + 8 \times 10 + 7 \times 1 \\ &= 200 + 80 + 7 \end{aligned}$$

This is called **expanded form**.

Example 3 **Converting Standard Form to Expanded Form**

Convert to expanded form.

a. 4,672 **b.** 257,016

Solution:

a. 4,672

$$\begin{aligned} &4 \text{ thousands} + 6 \text{ hundreds} + 7 \text{ tens} + 2 \text{ ones} \\ &= 4 \times 1{,}000 + 6 \times 100 + 7 \times 10 + 2 \times 1 \\ &= 4{,}000 + 600 + 70 + 2 \end{aligned}$$

b. 257,016

$$\begin{aligned} &2 \text{ hundred-thousands} + 5 \text{ ten-thousands} + \\ &7 \text{ thousands} + 1 \text{ ten} + 6 \text{ ones} \\ &= 2 \times 100{,}000 + 5 \times 10{,}000 + 7 \times 1{,}000 + 1 \times 10 + 6 \times 1 \\ &= 200{,}000 + 50{,}000 + 7{,}000 + 10 + 6 \end{aligned}$$

Skill Practice Convert to expanded form.

5. 837 **6.** 4,093,062

Answers

4. 5: hundred-thousands
7: ten-thousands
1: thousands 9: hundreds
6: tens 2: ones

5. 8 hundreds + 3 tens + 7 ones;
$8 \times 100 + 3 \times 10 + 7 \times 1$

6. 4 millions + 9 ten-thousands + 3 thousands + 6 tens + 2 ones;
$4 \times 1{,}000{,}000 + 9 \times 10{,}000 + 3 \times 1{,}000 + 6 \times 10 + 2 \times 1$

Example 4 **Converting Expanded Form to Standard Form**

Convert to standard form.

a. 2 hundreds + 5 tens + 9 ones

b. 1 thousand + 2 tens + 5 ones

Solution:

a. 2 hundreds + 5 tens + 9 ones = 259

b. Each place position from the thousands place to the ones place must contain a digit. In this problem, there is no reference to the hundreds place digit. Therefore, we assume 0 hundreds. Thus,

1 thousand + 0 hundreds + 2 tens + 5 ones = 1,025

Skill Practice Convert to standard form.

7. 8 thousands + 5 hundreds + 5 tens + 1 one

8. 5 hundred-thousands + 4 thousands + 8 tens + 3 ones

3. Writing Numbers in Words

The word names of some two-digit numbers appear with a hyphen, while others do not. For example:

Number	Number Name
12	twelve
68	sixty-eight
40	forty
42	forty-two

To write a three-digit or larger number, begin at the leftmost group of digits. The number named in that group is followed by the period name, followed by a comma. Then the next period is named, and so on.

Example 5 **Writing a Number in Words**

Write 621,417,325 in words.

Solution:

621,417,325

six hundred twenty-one million,

four hundred seventeen thousand,

three hundred twenty-five

Skill Practice

9. Write 1,450,327,214 in words.

Answers

7. 8,551 **8.** 504,083

9. One billion, four hundred fifty million, three hundred twenty-seven thousand, two hundred fourteen

Notice from Example 5 that when naming numbers, the name of the ones period is not attached to the last group of digits. Also note that for whole numbers, the word *and* should not appear in word names. For example, 405 should be written as four hundred five.

Example 6 Writing a Number in Standard Form

Write the number in standard form.

Six million, forty-six thousand, nine hundred three

Solution:

six million — nine hundred three

6,046,903

forty-six thousand

Skill Practice

10. Write the number in standard form: fourteen thousand, six hundred nine.

We have seen several examples of writing a number in standard form, in expanded form, and in words. Standard form is the most concise representation. Also note that when we write a four-digit number in standard form, the comma is often omitted. For example, 4,389 is often written as 4389.

4. The Number Line and Order

Whole numbers can be visualized as equally spaced points on a line called a *number line* (Figure 1-2).

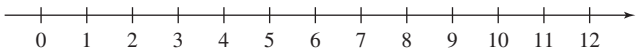
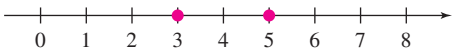


Figure 1-2

The whole numbers begin at 0 and are ordered from left to right by increasing value.

A number is graphed on a number line by placing a dot at the corresponding point. For any two numbers graphed on a number line, the number to the left is less than the number to the right. Similarly, a number to the right is greater than the number to the left. In mathematics, the symbol $<$ is used to denote "is less than," and the symbol $>$ means "is greater than." Therefore,

$3 < 5$ means 3 is less than 5
$5 > 3$ means 5 is greater than 3



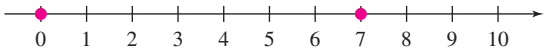
Example 7 Determining Order of Two Numbers

Fill in the blank with the symbol $<$ or $>$.

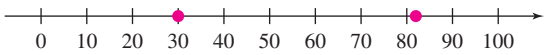
a. $7 \square 0$ **b.** $30 \square 82$

Solution:

a. $7 > 0$



b. $30 < 82$



To visualize 82 and 30 on the number line, it may be necessary to use a different scale. Rather than setting equally spaced marks in units of 1, we can use units of 10. Then 82 must be somewhere between 80 and 90 on the number line.

Skill Practice Fill in the blank with the symbol $<$ or $>$.

11. $9 \square 5$ **12.** $8 \square 18$

Answers

10. 14,609
11. $>$ **12.** $<$

Section 1.1 Activity

A.1. In a recent presidential election, the State of Wisconsin had 1,902,505 people request an absentee ballot.

a. Determine the place value of the underlined digit. 1,9̲02,505 _____

b. Convert 1,902,505 to expanded form.

c. Write 1,902,505 in words.

A.2. Of the 1,902,505 total absentee ballots requested in Wisconsin, one million, eight hundred ninety-six thousand, five hundred thirty-one ballots were sent to voters. Write this number in standard form.

For Exercises A.3–A.6:

a. Write two true inequalities (one using > and one using <) for each pair of values given below.

b. Translate one of the inequalities to words.

A.3. 210 and 201

a. _____ or _____

b. _____

A.4. 2233 and 2323

a. _____ or _____

b. _____

A.5. 79 and 76

a. _____ or _____

b. _____

A.6. 614 and 641

a. _____ or _____

b. _____

A.7. Consider the numbers 5, 9, 2, and 7.

a. What is the greatest four-digit number that can be formed from the digits? Use each digit only once.

b. What is the smallest four-digit number that can be formed from the digits? Use each digit only once.

c. Write the number from part (b) in words.

Section 1.1 Practice Exercises

Study Skills Exercise

To enhance your learning experience, we provide study skills throughout this textbook that focus on three main areas: mindset (ability to learn new concepts, grit, and overcoming math anxiety), study habits (managing time, taking notes, and test preparation), and mastering mathematical concepts (writing mathematically, reading comprehension, and memory techniques).

Each activity requires only a few minutes and will help you pass this course and become a better math student. Many of these skills can be carried over to other disciplines and help you become a model college student. To begin, write down the following information:

a. Instructor's name

b. Instructor's office number

c. Instructor's telephone number

d. Instructor's email address

e. Instructor's office hours

f. Days of the week that the class meets

g. The room number in which the class meets

h. Is there a lab requirement for this course? If so, where is the lab located and how often must you go?

Vocabulary and Key Concepts

1. a. For large numbers, commas are used to separate digits into groups called _____.

b. The place values of the digits in the ones period are the ones, tens, and _____ places.

c. The place values of the digits in the _____ period are the thousands, ten-thousands, and hundred-thousands places.

Concept 1: Place Value

2. Name the place value for each digit in 36,791.

3. Name the place value for each digit in 8,213,457.

4. Name the place value for each digit in 103,596.

For Exercises 5–24, determine the place value for each underlined digit. **(See Example 1.)**

5. 3$\underline{2}$1

6. 6$\underline{8}$9

7. 21$\underline{4}$

8. 73$\underline{8}$

9. 8,$\underline{7}$10

10. 2,$\underline{2}$93

11. $\underline{1}$,430

12. $\underline{3}$,101

13. $\underline{4}$52,723

14. $\underline{6}$55,878

15. $\underline{1}$,023,676,207

16. $\underline{3}$,111,901,211

17. $\underline{2}$2,422

18. $\underline{5}$8,106

19. 5$\underline{1}$,033,201

20. 9$\underline{3}$,971,224

21. The number of U.S. travelers abroad in a recent year was $\underline{1}$0,677,881. **(See Example 2.)**

22. The area of Lake Superior is 3$\underline{1}$,820 square miles (mi^2).

Morey Milbradt/Getty Images

23. For a recent year, the total number of U.S. $1 bills in circulation was $\underline{7}$,653,468,440.

24. For a certain flight, the cruising altitude of a commercial jet is $\underline{3}$1,000 ft.

Concept 2: Standard Notation and Expanded Notation

For Exercises 25–32, convert the numbers to expanded form. **(See Example 3.)**

25. 58

26. 71

27. 539

28. 382

29. 5,203

30. 7,089

31. 10,241

32. 20,873

For Exercises 33–40, convert the numbers to standard form. **(See Example 4.)**

33. 5 hundreds + 2 tens + 4 ones

34. 3 hundreds + 1 ten + 8 ones

35. 1 hundred + 5 tens

36. 6 hundreds + 2 tens

37. 1 thousand + 9 hundreds + 6 ones

38. 4 thousands + 2 hundreds + 1 one

39. 8 ten-thousands + 5 thousands + 7 ones

40. 2 ten-thousands + 6 thousands + 2 ones

41. Name the first four periods of a number (from right to left).

42. Name the first four place values of a number (from right to left).

Concept 3: Writing Numbers in Words

For Exercises 43–50, write the number in words. **(See Example 5.)**

43. 241

44. 327

45. 603

46. 108

47. 31,530

48. 52,160

49. 100,234

50. 400,199

51. The Shuowen jiezi dictionary, an ancient Chinese dictionary that dates back to the year 100, contained 9535 characters. Write 9535 in words.

52. Interstate I-75 is 1377 miles (mi) long. Write 1377 in words.

53. The altitude of Denali in Alaska is 20,310 ft. Write 20,320 in words.

54. There are 1800 seats in a theater. Write 1800 in words.

55. Researchers calculate that about 590,712 stone blocks were used to construct the Great Pyramid. Write 590,712 in words.

56. In the United States, there are approximately 60,000,000 cats living in households. Write 60,000,000 in words.

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For Exercises 57–62, convert the number to standard form. **(See Example 6.)**

57. Six thousand, five

58. Four thousand, four

59. Six hundred seventy-two thousand

60. Two hundred forty-eight thousand

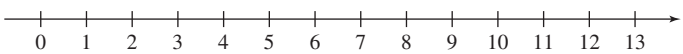
61. One million, four hundred eighty-four thousand, two hundred fifty

62. Two million, six hundred forty-seven thousand, five hundred twenty

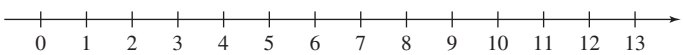
Concept 4: The Number Line and Order

For Exercises 63 and 64, graph the numbers on the number line.

63. **a.** 6 **b.** 13 **c.** 8 **d.** 1



64. **a.** 5 **b.** 3 **c.** 11 **d.** 9



65. On a number line, what number is 4 units to the right of 6?

66. On a number line, what number is 8 units to the left of 11?

67. On a number line, what number is 3 units to the left of 7?

68. On a number line, what number is 5 units to the right of 0?

For Exercises 69–72, translate the inequality to words.

69. $8 > 2$

70. $6 < 11$

71. $3 < 7$

72. $14 > 12$

For Exercises 73–84, fill in the blank with the inequality symbol $<$ or $>$. **(See Example 7.)**

73. $6 \square 11$

74. $14 \square 13$

75. $21 \square 18$

76. $5 \square 7$

77. $3 \square 7$

78. $14 \square 24$

79. $95 \square 89$

80. $28 \square 30$

81. $0 \square 3$

82. $8 \square 0$

83. $90 \square 91$

84. $48 \square 47$

Expanding Your Skills

85. Answer true or false. 12 is a digit.

86. Answer true or false. 26 is a digit.

87. What is the greatest two-digit number?

88. What is the greatest three-digit number?

89. What is the greatest whole number?

90. What is the least whole number?

91. How many zeros are there in the number ten million?

92. How many zeros are there in the number one hundred billion?

93. What is the greatest three-digit number that can be formed from the digits 6, 9, and 4? Use each digit only once.

94. What is the greatest three-digit number that can be formed from the digits 0, 4, and 8? Use each digit only once.

Addition and Subtraction of Whole Numbers and Perimeter

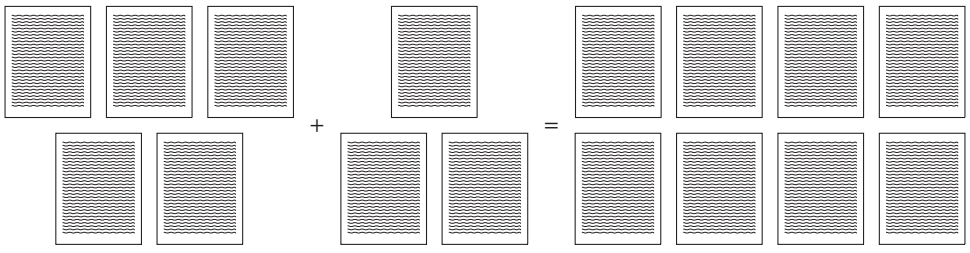
Section 1.2

1. Addition of Whole Numbers

Concepts

We use addition of whole numbers to represent an increase in quantity. For example, suppose Jonas typed 5 pages of a report before lunch. Later in the afternoon he typed 3 more pages. The total number of pages that he typed is found by adding 5 and 3.

5 pages + 3 pages = 8 pages



The result of an addition problem is called the **sum**, and the numbers being added are called **addends**. Thus,

$$\underset{\text{addends}}{5 + 3} = \underset{\text{sum}}{8}$$